

⑧ Introduction of Parsers

A parser for any grammar is a program (and parsing is a technique) that takes as input string ' w ' and produces as output either a parser tree for w ,

if w is a valid sentence of grammar, or an error message indicating that w is not a valid sentence of given grammar.

There are two ways of identifying an elementary subtree.

(a) By deriving a string from a non-terminal, or.

(b) By reducing a string of symbols to a non-terminal.

Based on these two fundamental approaches to parsing namely:

(i) Top Down Parsing (TDP)

(ii) Bottom up Parsing (BUP)

are defined.

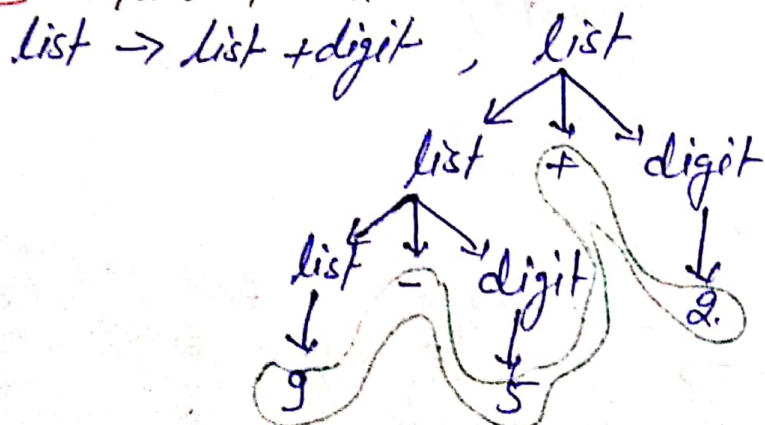
Example:- The production rule of grammar G is:

$list \rightarrow list + digit / list - digit / digit$

$digit \rightarrow 0 / 1 / 2 / \dots / 9$.

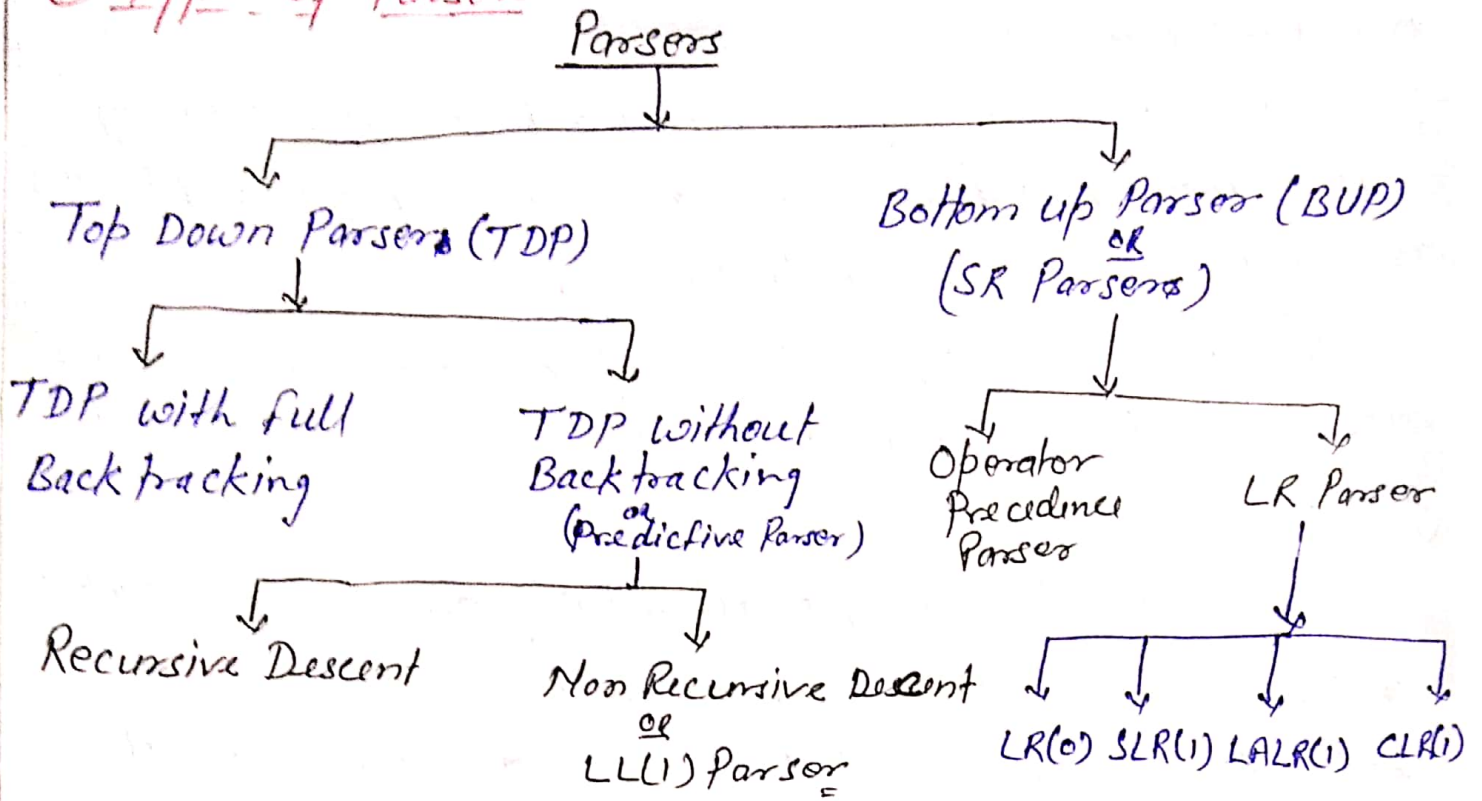
then find the parse tree for the expression: $9-5+2$.

Solution:- Parse tree is:



$= 9-5+2$ ✓ Ans

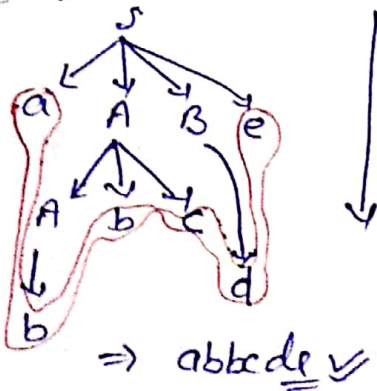
* Types of Parsers



* Basic Difference Between TDP and BUP:-

Example:- $S \rightarrow aABe$
 $A \rightarrow Abc/b$
 $B \rightarrow d$
 for $w = \underline{abbcde}$

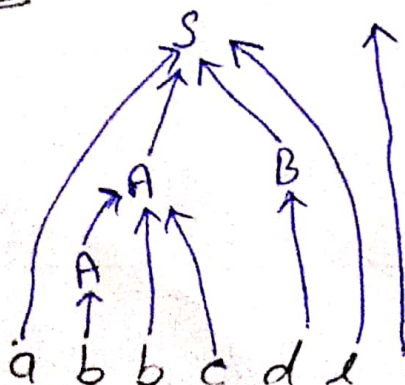
Soln:- TDP



\Rightarrow

$S \rightarrow a \underline{A} B e$	}	TDP is also used LMD.
$\rightarrow a \underline{A} b c B e$		
$\rightarrow a b b c \underline{B} e$		
$\rightarrow a b b c d e$		

BUP



\Rightarrow

$S \rightarrow a A B e$	}	BUP is use Reverse of RMD.
$\rightarrow a \underline{A} d e$		
$\rightarrow a \underline{A} b c d e$		
$\rightarrow a b b c d e$		

* Top Down Parsing:-

Basically top-down parsing attempts to find the left most derivations (LMD) for the input string w , since string w is scanned by the parser. Left to Right, one symbol / token at a time, and the LMD generate the leaves of the parse tree in left to right order, which matches the input scan order.

Example:- Consider the following grammar

$$V_n = \{ \text{expr, term, rest} \}$$

$$V_t / \Sigma = \{ +, -, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, \epsilon \}$$

$$\text{expr} \rightarrow \text{term rest}$$

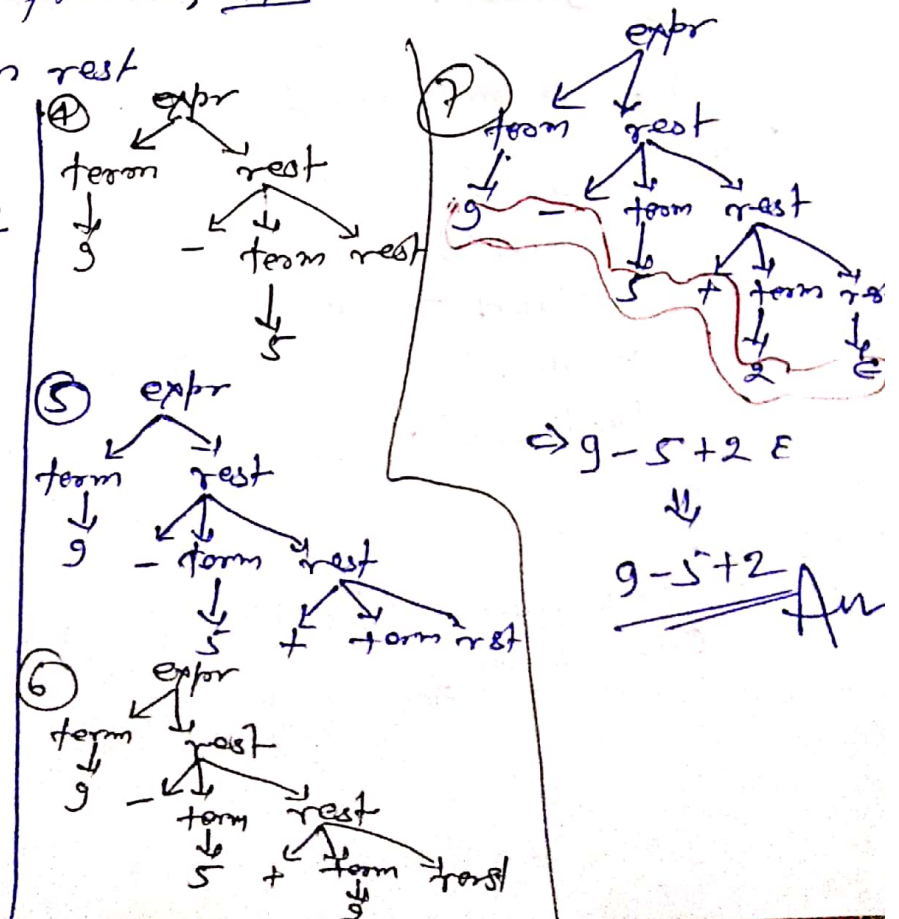
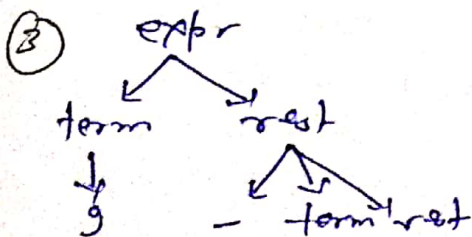
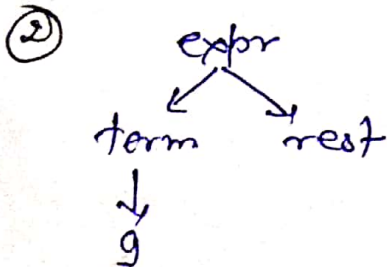
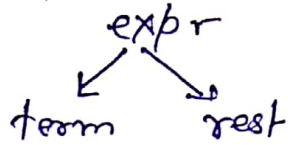
$$\text{rest} \rightarrow + \text{term rest} / - \text{term rest} / \epsilon$$

$$\text{term} \rightarrow 0 / 1 / 2 / 3 / 4 / 5 / 6 / 7 / 8 / 9$$

and show the construction of the parse tree for i/p string: 9-5+2.

Soln:- Initialization:- The root of parse tree must be starting s/b (non-terminal of the G), expr

Step 1 - $\text{expr} \rightarrow \text{term rest}$



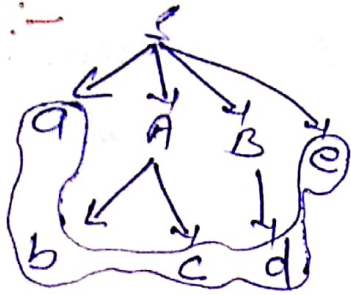
Example: $S \rightarrow aABe$

$A \rightarrow bc$

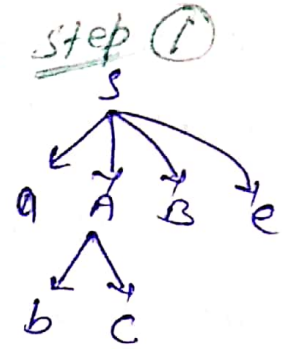
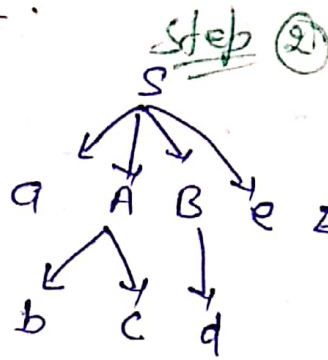
$B \rightarrow d$

and show the construction of parse tree for ~~TDP~~ for i/p $w = abcde$.

Soln: :-



= abcde Aug



* Recursive Descent Parsing :-

A TDP that executes a set of recursive ~~product~~ procedures to process the input ~~with~~ without backtracking is called recursive-descent parser, and parsing is called recursive descent parsing.

Example: suppose i/p stream is: $a + b \$$

i/p stream: $a + b \$$

Then

Lookhead == a

match ()

lookhead == +

match ()

lookhead == b

in this manner parsing can be done.

Example:- Write a code for recursive-descent parsing of the following grammar:

$expr \rightarrow term\ rest$

$rest \rightarrow +term\ rest \mid -term\ rest \mid \epsilon$

$term \rightarrow 0 \mid 1 \mid \dots \mid 9$

Solⁿ:- We know that in a recursive-descent parsing, we write code for each non-terminal of a grammar.

in the above grammar, we should have three procedures correspond to non-terminal: $expr$, $rest$, $term$.

there is only one procedure for non-terminal: $expr$.

the procedure $expr$ is:

```
expr()
{
    term();
    rest();
    return;
}
```

procedure $rest$ uses a global variable is "lookhead" to select correct production or simply select no action. $\epsilon \in$

```
rest()
{
    if (lookhead == '+')
    {
        match();
        term();
        rest();
        return;
    }
    else if (lookhead == '-')
    {
        match();
        term();
        rest();
        return;
    }
    else
    {
        return;
    }
}
```

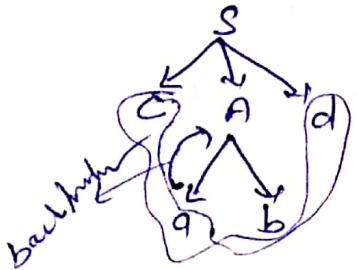
The procedure $term$ check whether global variable is a digit.

```
term() {
    if (is digit (lookhead))
    {
        match();
        return;
    }
    else
    {
        Error();
    }
}
```

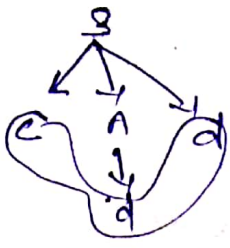

⊛ Backtracking :- The parse tree is started from root node and input string is matched against production rules for replacing them.

Example:- Let grammar G be
 $S \rightarrow cAd$
 $A \rightarrow ab|d$
 i/p string $w = cdd$.

Soln:- $S \rightarrow cAd$



$= cabd \neq cdd$ so had backtracking, and use another production rule.

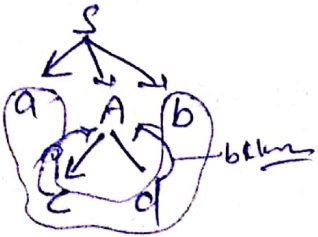


$= cdd = cdd \checkmark$ Ans

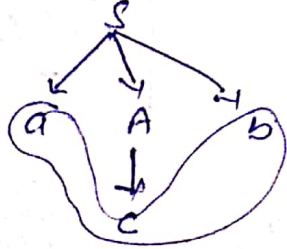
Example:- Consider the given grammar

$S \rightarrow aAb$
 $A \rightarrow cd|c$ and show the backtracking for string $w = \underline{acb}$.

Soln:- $S \rightarrow aAb$



=



$= \underline{acb}$ Ans

* Top down Parser / Top down Predictive Parser / LLL1

A predictive parser is an efficient way of implementing recursive-descent parsing since a stack is maintained in predictive parsing for handling the activation records.

In top down predictive parsers, the grammar will be able to predict the right alternative for the expansion of non-terminal during the parsing process; and hence, it need no backback.

Note → The parser is initialized with the start symbol of grammar on the stack top and the input pointing to the first token.

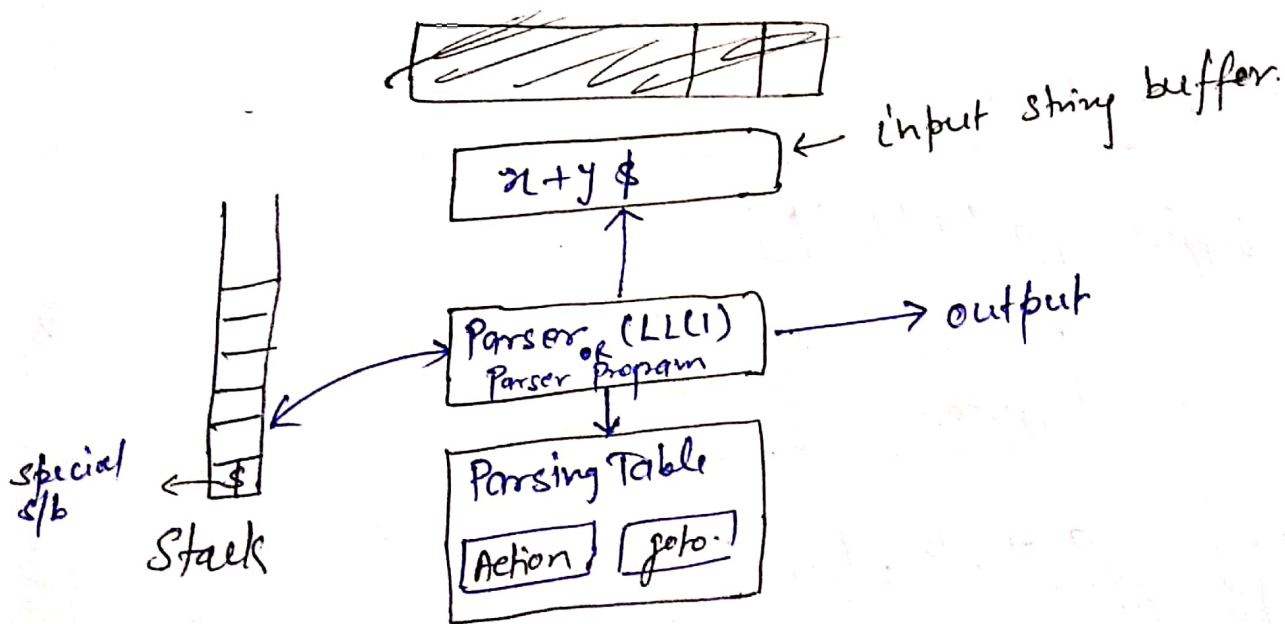


Fig: Predictive Parser

⇒ The action of the parser depends on the grammar symbol on the top of the stack,

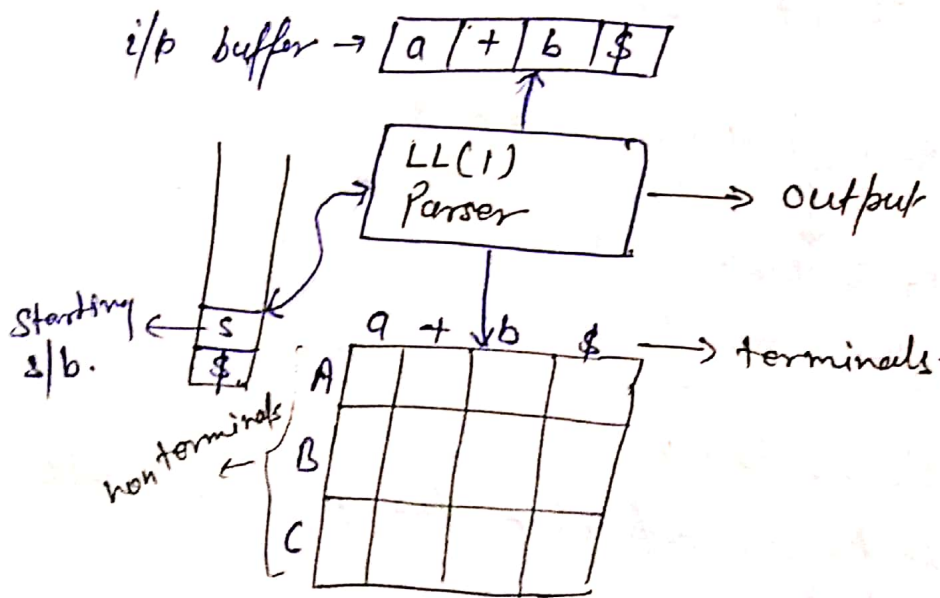
* LL(1) Parser :-

- it accepts LL grammars.
- it is denoted as LL(R)

• A grammar G is LL(1) if there are two distinct productions. eg:- $A \rightarrow \alpha/\beta$

- conditions:
- (i) for no terminal a and β derive string beginning with 'a'.
 - (ii) At most one of α and β can derive empty string.
 - (iii) if $\beta \rightarrow \epsilon$ then 'a' does not derive any string beginning with 'a' terminal in FOLLOW(A).

Structure of LL(1) :-



* Construction of Predictive of LL(1) :-

- (1) FIRST(C)
- FOLLOW(C)
- (2) Predictive parsing table by using first & follow functions.
- (3) Stack Implementation
- (4) Parse the input stream with the help of the table.

⊗ finding FIRST and FOLLOW:-

(i) FIRST function:-

- First(α) is a set of terminal symbol that begins in strings derived from α / production rule.

eg:- $A \rightarrow abc / def / ghi$

then

$$\text{first}(A) = \{a, d, g\}$$

OR

first() :- is a function which gives the set of terminals that begin the strings derived from the production rule.

- A symbol 'c' is in $\text{FIRST}(\alpha)$ if and only if $\alpha \Rightarrow c\beta$ for some sequence β of grammar symbols.

⊗ Rules for calculating first function:-

Algorithm to calculate the first(X) for a Grammar Symbol X .

- Rule
- ① if X is a terminal, $\text{first}(X)$ is $\{X\}$. (i.e. $\text{first}(X) = \{X\}$)
 - ② if $X \rightarrow \epsilon$ is a production, then add ϵ to the set of $\text{first}(X)$.
 - ③ if X is a non-terminal, $X \rightarrow Y$
 - (i) - if $\epsilon \notin \text{first}(Y)$ is an element of the set of $\text{first}(X)$
(e.g. $\text{first}(X) = \text{first}(Y)$)
 - (ii) if $\epsilon \in \text{first}(Y)$, and $X \rightarrow YZ$ then
 $\text{first}(X) = \text{first}(Y) - \{\epsilon\} \cup \text{first}(Z)$

Example: - if given grammar is

$$E \rightarrow TA$$

$$A \rightarrow +TA / \epsilon$$

$$T \rightarrow FB$$

$$B \rightarrow *FB / \epsilon$$

$$F \rightarrow (E) | id$$

then let us calculate $first(E)$, $first(A)$, $first(T)$, $first(B)$ and $first(F)$.

Solution: - $first(E) = first(TA)$ (since $E \rightarrow TA$)
 $= first(T)$
 $= first(FB)$
 $= first(F)$
 $= \{ (, id \}$

$$first(A) = \{ +, \epsilon \}$$

$$first(T) = \{ (, id \}$$

$$first(B) = \{ *, \epsilon \}$$

$$first(F) = \{ (, id \}$$

Ans

* Follow function:-

Follow function is a function which gives the set of terminals that ~~begin the strings derived from the production rule~~ that can appear immediately to the right of a given symbol.

A terminal symbol a is in $\text{follow}(N)$ if and only if there is a derivation from the start symbol S of the grammar such that $S \rightarrow \alpha N \beta$, where α and β are (possibly empty) sequences of grammar symbols.

OR

In other words, a terminal c is in $\text{follow}(N)$ if c may follow N at some point in a derivation.

* Rules for calculating follow function:-

①

Algorithm to calculate the follow(x) for a non-terminal X.

Rule ①:- $\$$ is an element of $\text{follow}(S)$, where S is the ~~the~~ start symbol and $\$$ indicates the end of the input.

Rule ②:- if $A \rightarrow \alpha X$ or $A \rightarrow \alpha XY$ are productions, and $\text{first}(Y)$ has an element ϵ , then set $\text{follow}(X)$ is in the set $\text{follow}(A)$.
is $\boxed{\text{follow}(X) = \text{follow}(A)}$

Rule ③:- if $A \rightarrow \alpha XY$ is a production, the set $\text{first}(Y)$ is in the set $\text{follow}(X)$, excluding ϵ .

Example:- Calculate the ^{first} follow of given grammar.
if given grammar is:

$$\begin{aligned} E &\rightarrow TA \\ A &\rightarrow +TA/\epsilon \\ T &\rightarrow FB \\ B &\rightarrow *FB/\epsilon \\ F &\rightarrow (E)/id \end{aligned}$$

Solution:- Now calculate first of A, E, T, B, F.

if $E \rightarrow TA$, then $\text{first}(E) = \{ (, id \}$

$A \rightarrow +TA/\epsilon$, then $\text{first}(A) = \{ +, \epsilon \}$

$T \rightarrow FB$, then $\text{first}(T) = \{ (, id \}$

$B \rightarrow *FB$; then $\text{first}(B) = \{ *, \epsilon \}$

$F \rightarrow (E)/id$; then $\text{first}(F) = \{ (, id \}$

Now calculate follow of E, A, T, B, F -

$$\text{follow}(E) = \{ \$,) \}$$

$$\text{follow}(A) = \{ \$,) \}$$

$$\begin{aligned} \text{follow}(T) &= \{ \text{first}(A) - \epsilon \} \cup \text{follow}(E) \\ &= \{ +, \epsilon - \epsilon \} \cup \{ \$,) \} \\ &= \{ +, \$,) \} \end{aligned}$$

$$\begin{aligned} \text{follow}(B) &= \text{follow}(T) \\ &= \{ +, \$,) \} \end{aligned}$$

$$\begin{aligned} \text{follow}(F) &= \{ \text{first}(B) - \epsilon \} \cup \text{follow}(T) \cup \text{follow}(B) \\ &= \{ *, \epsilon - \epsilon \} \cup \{ +, \$,) \} \cup \{ +, \$,) \} \\ &= \{ *, +, \$,) \} = \underline{\underline{Ans}} \end{aligned}$$