

Losses in transformer

a) Iron or Core loss (P_i)

b) Copper or I^2R loss (P_c)

a) Iron loss occur in magnetic core of transformer.

It is sum of hysteresis loss (P_h) and eddy current loss (P_e)

$$P_i = P_h + P_e$$

$$P_h = K_h f B_m^\alpha$$

$$P_e = K_e f^2 B_m^2$$

here

f = freq. of alternating f

B_m = max. flux density in C

K_h = Proportionality Constant depend on the volume and quality of core material and units used

K_e = Proportionality Constant whose value depends upon volume & resistivity of core material, thickness of lamination & units used

Exponent α called Steinmetz Constant. Its value varies from 1.5 to 2.5 depending upon magnetic properties of core material. The total core loss —

$$P_i = P_h + P_e$$

$$P_i = K_h f B_m^\alpha + K_e f^2 B_m^2$$

P_h depends on
→ applied V_{tg} & freq

P_e → depends on
* Square of applied V_{tg}
* Independent of fr.

Copper loss or I^2R loss (P_c)

I^2R loss take place in Primary & Secondary winding because of winding resistances.

$$\text{Total Cu loss in } \varnothing \text{ xmer} = \text{Primary wdg Cu loss} + \text{Secondary wdg Cu loss}$$

(Copper loss varies as the square of load current)

Separation of hysteresis & eddy current loss

$$\therefore P_i = P_h + P_e$$

$$P_i = k_h f B_m^2 + k_e f^2 B_m^2 \quad \text{--- (1)}$$

k_h = Constant whose value depend on ferromagnetic material

B_m = max. value of flux density

f = Supply freq.

* $x \rightarrow$ varies in (1.5 to 2.5 depend on material.)

for given B_m , P_h varies directly as freq. f

P_e varies as square of freq. i.e.

$$* P_h \propto f \quad \text{or} \quad P_h = a f$$

$$* P_e \propto f^2 \quad \text{or} \quad P_e = b f^2 \quad * a, b \text{ are constants}$$

$$\therefore \boxed{P_i = a f + b f^2}$$

for separation of these (2) losses the no-load test is performed on the xmer. however, primary of xmer is connected to a variable freq. & variable sinusoidal supply & secondary is open circuited.

$$\text{Now } V \approx E = 4.44 f \Phi_m N$$

$$\text{or } \frac{V}{f} = 4.44 B_m \cdot A \cdot N$$

for any xmer N & A are constants, therefore B_m will remain constant if the test is conducted so that the ratio (V/f) kept constant.

Divide eqⁿ by f ,

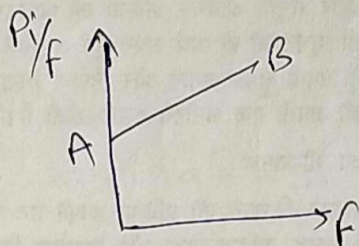
$$\boxed{\frac{P_i}{f} = bf + a}$$

Dummy test, v & f varied together so (v/f) is kept constant. & Core loss is obtained at diff freq.

A graph (P_i/f) versus freq. f is plotted.

Graph is straight line AB of form $y = mx + c$

Intercept of straight line on vertical axis gives a & slope of line AB gives b .



a & b are P_m & P_e constants.

Ex! In a core, $P_i = 100\text{W}$ at 40Hz & 72W at 30Hz .
Find P_m & P_e at 50Hz .

Solⁿ
$$\frac{P_i}{f} = a + bf$$

$$\frac{100}{40} = a + 40b \quad \& \quad \frac{72}{30} = a + 30b$$

by solving $\rightarrow a = 2.1$ & $b = 0.01$

therefore

$$P_m \text{ at } 50\text{Hz} \rightarrow a f = 2.1 \times 50 = \boxed{105\text{W}}$$

$$P_e \text{ at } 50\text{Hz} \rightarrow bf^2 = 0.01 \times 50^2 = \boxed{25\text{W}}$$