

Tension Member

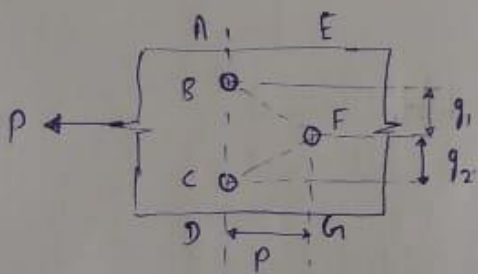
- Pulling force is applied in the opposite dirⁿ at the two ends of the member.
- Bending stress due to self wt. is neglected.

Critical tensile stress and critical c/s area →

- Critical tensile stress in a tension member occurs at the section where the c/s area is minimum. So No. of Bolts/Rivets and arrangement of them affect the c/s area.

Area Calculation →

* Net Area calculation for plate section →



Possible failure Plane

- ✓ ABCD
 - ✓ ABFC D
 - x EFG
 - x ABFC D
- } → Possible

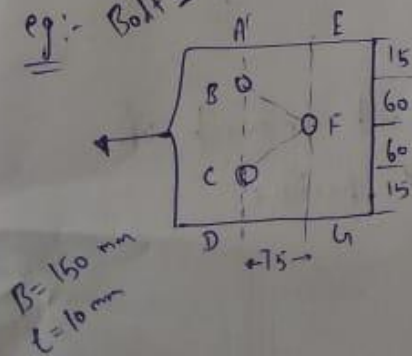
$$ABCD \rightarrow (B - 2d_o)t$$

$$ABFC D \rightarrow \left(B - 3d_o + \frac{p^2}{4g_1} + \frac{p^2}{4g_2} \right) t$$

$$\left. \begin{matrix} A_1 \\ A_2 \end{matrix} \right\} \text{min. } \cong$$

[From IS 800:2007]
 $P_y = 33$

eg:- Bolt dia. = 20 mm



$$\text{Gross Area} = 150 \times 10 = 1500 \text{ mm}^2$$

$$ABCD = (150 - 2 \times 21.5) \times 10 = 1070 \text{ mm}^2$$

$$(d_o = 1.5d)$$

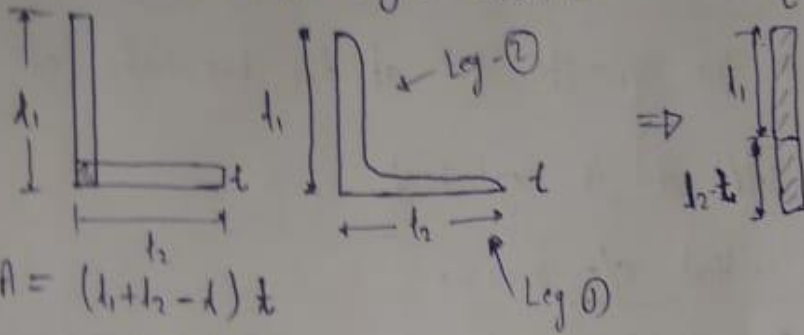
$$ABFC D = \left(150 - 3 \times 21.5 + \frac{75^2}{4 \times 60} + \frac{75^2}{4 \times 60} \right) \times 10$$

$$EFG = (150 - 21.5) \times 10 = 1323.75 \text{ mm}^2$$

$$= 1285 \text{ mm}^2$$

So $A_{net} = 1070 \text{ mm}^2$ / And for critical c/s = ABCD

Area calculation for angle section →



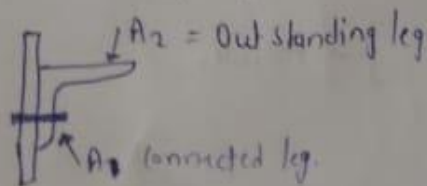
$$A = (l_1 + l_2 - t) t$$

$$A_1 = l_1 \times t - \frac{t \times t}{2} = (l_1 - \frac{t}{2}) t$$

$$A_2 = l_2 \times t - \frac{t \times t}{2} = (l_2 - \frac{t}{2}) t$$

$$\text{Total Area } A = A_1 + A_2 \\ = (l_1 + l_2 - t) t$$

eg:- ISA: $l_1 \times l_2 \times t$



$$A_1 = (l_1 - \frac{t}{2} - d) t$$

$$A_2 = (l_2 - \frac{t}{2}) t$$

Shear leg Effect → Non uniform stress distribution near the connection in case of angle sections is called as shear leg effect.

- To reduce it length of connection should be increased or unequal angle section should be provided.
- Provide gusset two gusset plates to eliminate shear leg.

Types of failure in tension members.

- (1) Yielding of gross section (T_{yg}) → Significant amount of deformation before ~~failure~~ fracture.
- (2) Rupture or fracture of net section (T_{dn})
- (3) Block shear failure (T_{db})

① T_{dg} The design strength due to yielding of the gross section is given by →

$$T_{dg} = \frac{A_g f_y}{\gamma_{mo}} \quad \left\{ \begin{array}{l} \text{IS: 800:2007} \\ \text{Cl. 6.2 } \gamma_{mo} = 1.25 \end{array} \right.$$

f_y → Yield stress of material

A_g → Gross area of c/s

γ_{mo} → Partial safety factor [Table - No. = 5 IS : 800]

② Design strength due to rupture of Net section (T_{dn})

(i) In case of plates →

$$T_{dn} = 0.9 \frac{A_n f_u}{\gamma_{m1}} \quad \left\{ \begin{array}{l} \text{IS 800:2007} \\ \gamma_{m1} = 1.25 \end{array} \right.$$

f_u → Ultimate stress of material

A_n → Net eff. area

$$A_n = \left[b - n d_o + \sum \frac{P_i^2}{4g_i} \right] t \quad \left\{ \begin{array}{l} P \rightarrow \text{Pitch} \\ g \rightarrow \text{Gauge} \end{array} \right.$$

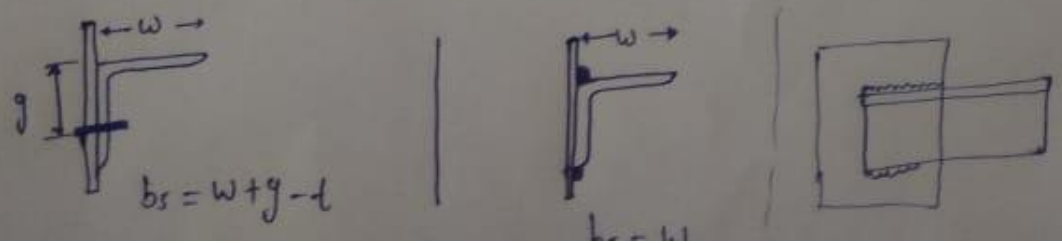
(ii) Single angle →

$$T_{dn} = 0.9 \frac{A_{nc} f_u}{\gamma_{m1}} + \beta A_{go} \frac{f_y}{\gamma_{mo}}$$

where $\beta = 1.4 - 0.076 (w/t) (f_y/f_u) (b_s/L_c) \leq \begin{cases} 1.0 \\ \gamma_{mo} / \gamma_{m1} \end{cases} \geq 0.7$

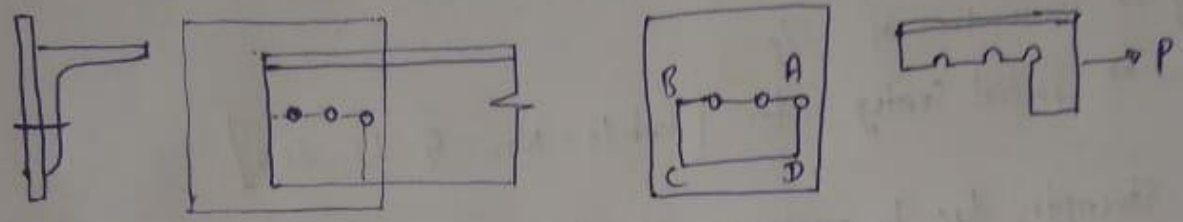
w → Outstanding leg width
 b_s → Shear leg width

Case - I



Block Shear strength $\rightarrow (T_{db})$

- It is combination of shear and tensile strength of member under tensile forces.
- Block shear strength depends upon end distance & pitch distance.



Bolt Shear Strength \rightarrow

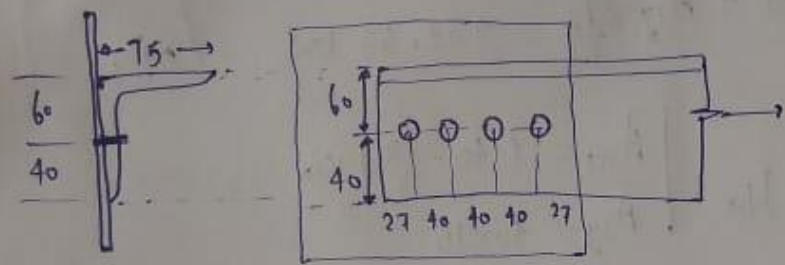
$$\left[T_{db} = \frac{A_{vg} f_y}{\sqrt{3} \gamma_{mo}} + 0.9 A_{Tn} \frac{f_u}{\gamma_{m1}} \right]$$

$$\left[T_{db} = 0.9 \frac{A_{vn} f_u}{\sqrt{3} \gamma_{m1}} + A_{Tg} \frac{f_y}{\gamma_{mo}} \right] \text{ min}^m$$

$$\left[\begin{aligned} A_{vg} &= AB \times t \\ A_{sn} &= (AB - d_o - d_o - \frac{d_o}{2}) t \\ A_{Tg} &= AD \times t \\ A_{Tn} &= (AD - \frac{d_o}{2}) t \end{aligned} \right] \text{ from above diagram.}$$

\Rightarrow Tensile strength of member (T_d) is the min^m of T_{dg} , T_{dn} & T_{db} .

Q. Calculate tensile strength of the angle ISA 100x75x10 for the given arrangement. 16mm dia bolts are used to make the connection.



$d = 16\text{mm}$
 $\therefore d_o = 18\text{mm}$

(1) Yielding of gross section

$$\begin{aligned} \text{Gross Strength} &= A_g \times \frac{f_y}{1.1} \\ &= (l_1 + l_2 - t) t \times \frac{250}{1.1} = (100 + 75 - 10) \times 10 \times \frac{250}{1.1} \\ T_{dg} &= 375 \text{ kN} \end{aligned}$$

{ IS : 800 : 2007 }
 $f_y = 250$

(2) Net tensile strength

$$\begin{aligned} T_{dN} &= A_{nc} \times \frac{f_u}{1.25} \times 0.9 + \beta A_{go} \times \frac{f_y}{1.1} \\ A_{nc} &= (l_1 - \frac{t}{2} - d_o) t \\ &= (100 - \frac{10}{2} - 18) 10 = 1130 \text{ mm}^2 \\ A_{go} &= (l_2 - \frac{t}{2}) t = (75 - 5) \times 10 = 700 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} \beta &= 1.4 - 0.076 \left(\frac{w}{t} \right) \left(\frac{f_y}{f_u} \right) \left(\frac{b_s}{L_c} \right) \\ b_s &= w + g - t, \quad L_c = 120 \text{ mm} \\ &= 75 + 60 - 10 \\ &= 125 \text{ mm} \end{aligned}$$

$$\begin{aligned} \beta &= 1.4 - 0.076 \left(\frac{75}{10} \right) \left(\frac{250}{410} \right) \left(\frac{125}{120} \right) \\ \beta &= 1.037 \end{aligned}$$

$$\begin{aligned} T_{dN} &= 1130 \times \frac{410}{1.25} \times 0.9 + 1.037 \times 700 \times \frac{250}{1.1} \\ &= 392.5 \text{ kN} \end{aligned}$$

(3) Block Shear Strength

$$T_{db} = \frac{A_{sv}}{\sqrt{3}} \times \frac{f_y}{1.1} + A_{TN} \times \frac{f_{yp}}{1.25} \times 0.9 = 284.39 \text{ kN}$$

$$\textcircled{6y} \quad = \frac{A_{sN}}{\sqrt{3}} \times \frac{f_{yp}}{1.25} \times 0.9 + A_{Ty} \times \frac{f_y}{1.1} = 234.67 \text{ kN}$$

} min.

$$A_{sv} = 147 \times t_0$$

$$A_{sN} = (147 - 18 - 18 - 18 - \frac{18}{2}) t_0$$

$$A_{TN} = (40 - \frac{18}{2}) \times 10$$

$$A_{Ty} = 40 \times 10$$

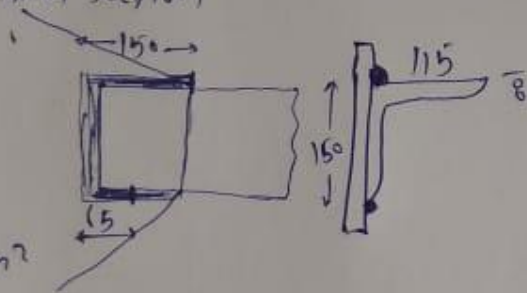
$$T_{db} = 234.67 \text{ kN}$$

So Design tensile strength $T_d = \underline{234.67 \text{ kN}}$

Q. Determine the tensile strength of an angle section ISA 150x115x8 which is connected to gusset plate for the following cases: Use Fe410

- (1) Yielding of gross-section
- (2) Rupture strength of critical section

Sol.:



$$A_g = 150 \times 115 \times 8 = 2058 \text{ mm}^2$$

(1) T_{dy} = Tensile strength due to gross-section \rightarrow

$$T_{dy} = \frac{A_g f_y}{\gamma_{mo}} = \frac{2058 \times 250}{1.1} = 467.73 \text{ kN}$$

(2) Rupture strength (T_{dn}) \rightarrow

$$T_{dn} = \frac{0.9 A_{nc} f_u}{\gamma_{m1}} + \beta \frac{A_{go} f_y}{\gamma_{mo}}$$

$$A_{nc} = (150 - \frac{8}{2}) \times 8 = 1168 \text{ mm}^2$$

$$A_{go} = (115 - \frac{8}{2}) \times 8 = 888 \text{ mm}^2$$

$$\beta = 1.4 - 0.076 \left(\frac{w/t}{t} \right) \left(\frac{f_y}{f_u} \right) \left(\frac{b_s/l_c} \right) \leq \frac{0.9 f_u \gamma_{mo}}{f_y \gamma_{m1}} \geq 0.7$$

$$= 1.4 - 0.076 \left(\frac{115}{8} \right) \left(\frac{250}{410} \right) \left(\frac{115}{150} \right) = 0.8893$$

$$\frac{0.9 f_u \gamma_{mo}}{f_y \gamma_{m1}} = \frac{0.9 \times 410 \times 1.1}{250 \times 1.25} = 1.2988 > 0.7$$

$$\beta = 0.8893$$

$$T_{dn} = 524.27 \text{ kN}$$